

score	possible	problem
	30	1
	20	2
	20	3
	30	4
	100	

Name: _____

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Work in groups of 3 or 4. Show your work. Acknowledge any help on these specific problems.

1. Compute the following derivatives:

/15 (a) $\frac{d}{dx} \sec(x \sin(x^2 + 1)) =$

/15 (b) $\frac{d}{dx} \left(x + \frac{1}{x^3 + 1} \right)^{\sqrt{7}} =$

- /20 2. Use implicit differentiation to find the equation of the tangent line to the curve defined by

$$x^2 + y^2 = (2x^2 + 2y^2 - x)^2$$

at the point $(0, 1/2)$.

- /10 3. (a) A cylindrical tank with radius 5m is being filled with water at a rate of $3\text{m}^3/\text{min}$.
- Draw and label a diagram illustrating this scenario.
 - Write an equation relating the volume of water in the tank and the height of water in the tank.
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- /10 (b) A plane flying horizontally at an altitude of 1km and speed of 500km/hr flies directly over a radar station.
- Draw and label a diagram illustrating this scenario.
 - Write an equation relating the horizontal distance from the plane to the radar station and the direct (diagonal) distance from the plane to the radar station,

- /15 4. (a) A man starts running north at 4m/s from a point P . Five minutes later a woman starts running south at 5m/s from a point 500m due east of P .
- Draw and label a diagram illustrating this scenario.
 - Write an equation relating the distance of the man from P , the distance of the woman from her starting point, and the distance from the man to the woman.

- /15 (b) A trough is 10m long and its ends have the shape of isosceles triangles that are 3m across at the top and have a height of 1m . The trough is being filled with water at a rate of $12\text{m}^3/\text{min}$.
- Draw and label a diagram illustrating this scenario.
 - Write an equation relating the volume of water in the trough and the height of water in the trough.